

SOLUTIONS

Math 51B Summer 2006

Name: _____

QUIZ #3 @ 20 points Section 3.4

Write neatly. Use a pencil. Label the axes and the points used. Show work in order to get credit. No proof, no credit given.

1. Write an equation of the line with slope 3 and y-intercept (0,-2). $y = mx + b$, $m = 3$
 $b = -2$

$$\boxed{y = 3x - 2}$$

2. a) Write an equation of the line passing through the point (1,2) and having slope 4.

$$y - y_1 = m(x - x_1), \text{ where } m = 4$$

$$(x_1, y_1) = (1, 2)$$

$$\boxed{y - 2 = 4(x - 1)}$$

- b) Write the equation in slope-intercept form.

$$y - 2 = 4(x - 1)$$

$$y - 2 = 4x - 4$$

$$y = 4x - 4 + 2$$

$$\boxed{y = 4x - 2}$$

- c) Write the equation in standard form.

$$y = 4x - 2$$

$$\boxed{-4x + y = -2}$$

$$\text{OR } \boxed{4x - y = 2}$$

3. Write an equation of the line passing through (-1,3) and (2,-5).

$$y - y_1 = m(x - x_1) \text{ with } (x_1, y_1) = (-1, 3)$$

Need $m = ?$

$$m = \frac{\Delta y}{\Delta x} = \frac{3 - (-5)}{-1 - 2} = \frac{3 + 5}{-3} = \frac{8}{-3}$$

$$m = \frac{8}{-3}$$

$$y - 3 = \frac{-8}{3}(x - (-1)) \Rightarrow \boxed{y - 3 = \frac{-8}{3}(x + 1)}$$

4. a) What is the slope of the line $2x + 5y = 7$?

$$2x + 5y = 7$$

$$5y = -2x + 7$$

$$\boxed{y = \frac{-2}{5}x + \frac{7}{5}} \text{ slope-intercept form}$$

$$\Rightarrow \boxed{m = \frac{-2}{5}}$$

- b) What is the slope of a line parallel to the line from part a)?

$$\boxed{m = \frac{-2}{5}}$$

(because $l_1 \parallel l_2 \Leftrightarrow m_1 = m_2$)

- c) What is the slope of a line perpendicular to the line from part a)?

$$m_{\perp} = \frac{-1}{m} = \frac{5}{2}$$

$$\boxed{m_{\perp} = \frac{5}{2}}$$

(because $l_1 \perp l_2 \Leftrightarrow m_1 = \frac{-1}{m_2}$)