Chapter 5 Polynomials, Polynomial Functions, and Factoring

- 1. Textbook #73 page 310 The common cold is caused by a rhinovirus. After x days of invasion by the viral particles, the number of particles in our bodies, $\underline{f(x)}$, in billions, can be modeled by the polynomial function $f(x) = -0.75x^4 + 3x^3 + 5$. Use the leading coefficient test to determine the graph's end behavior to the right. What does this mean about the number of viral particles in our bodies over time?
- 2. If $f(x) = x^2 3x + 7$, find each of the following and simplify:

a)
$$f(a+2)$$

b)
$$f(a+h)-f(a)$$

3. Simplify:
$$(y^n + 2)(y^n - 2) - (y^n - 3)^2$$

 $(A: 6y^n - 13)$

4. Factor each polynomials completely:

a)
$$2y^7 (3x-1)^5 -7y^6 (3x-1)^4$$

d)
$$x^{4n} + x^{2n} + x^{3n}$$

b)
$$ax + ay + az - bx - by - bz + cx + cy + cz$$
 e) $3x^{3m}y^m - 6x^{2m}y^{2m}$ g) $24x^2 + 3xy - 27y^2$

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c)
$$x^n y^n + 3x^n + y^n + 3$$

f)
$$15x^3 - 25x^2 + 10x$$

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 h) $4x^3y^5 + 24x^2y^5 - 64xy^5$

5. Factor by introducing an appropriate substitution.

a)
$$2x^4 - x^2 - 3$$

c)
$$3(x-2)^2 - 5(x-2) - 2$$

e)
$$a^{2n+2} - a^{n+2} - 6a^2$$

b)
$$2x^6 + 11x^3 + 15$$

d)
$$9x^{2n} + x^n - 8$$

6. Factor completely.

a)
$$x^2 - 0.5x + 0.06$$

c)
$$0.04x^2 + 0.12x + 0.09$$

e)
$$acx^2 - bcx + adx - bd$$

b)
$$x^2 - \frac{6}{25} + \frac{1}{5}x$$

d)
$$8x^4 - \frac{x}{8}$$

f)
$$x^5 - x^3 + 27x^2 - 27$$

7. If
$$(fg)(x) = 3x^2 - 22x + 39$$
, find f and g.

- 8. Textbook # 105 page 345 A diver jumps directly upward from a board that is 32 feet high. The function $f(t) = -16t^2 + 16t + 32$ describes the diver's height above the water, f(t), in feet, after t seconds.
- a) Find and interpret f(1).
- b) Find and interpret f(2).
- **9.** Factor completely:

a)
$$4a^3c^2 - 16ax^2y^2$$

d)
$$x^3 - 6x^2 - x + 6$$

g)
$$x^2 - 6x + 9 - y^2$$
 j) $216x - x^4$

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b)
$$8x^2 + 8y^2$$

e)
$$16x^2 - 40xy + 25y^2$$

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$$16x^2 - 40xy + 25y^2$$
 h) $25x^2 - 20x + 4 - 81y^2$ k) $x^9 + 1$

k)
$$x^9 + 1$$

c)
$$1 - 81x^4$$

f)
$$x^2 - 8xy + 64y^2$$

i)
$$125x^3 - 8$$

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 l) $x^3 + (x + y)^3$

10. Solve each equation by factoring.

a)
$$x^2 - 4x = 45$$
 (A: -5,-9)

e)
$$(2x-1)(3x+\frac{1}{2})(x-1)^2=0$$

b)
$$x^2 = 8x$$

f)
$$x^3 + 4x^2 - 25x - 100 = 0$$
 (A: -5, -4, 5)

c)
$$(x-3)(x+8) = -30$$
 (A: -3, -2)

g)
$$3x^4 - 48x^2 = 0$$

d)
$$\frac{x^2}{4} - \frac{5x}{2} + 6 = 0$$
 (A: 4, 6) h) $x(x+1)^3 - 42(x+1)^2 = 0$ (A: -7, -1, 6) i) $-7x[x(3x-2)-8](25x^2 - 40x + 16) = 0$ (A: -5/3, -3/2, 0, 4). j) $|x^2 + 2x - 36| = 12$ (A: -8, -6, 4, 6)

- 11. Find all numbers satisfying the given conditions:
- a) If 5 is subtracted from 3 times the number, the result is the square of 1 less than the number. (A: 2, 3)
- b) The product of the number decreased by 1 and increased by 4 is 24. (A:-7, 4)
- 12. Textbook # 67, 68 page 373 The function $f(x) = -\frac{1}{4}x^2 + 3x + 17$ models the number of people, f(x),

in millions, receiving food stamps x years after 1990.

a) In which year did 25 million people receive food stamps?

(A: 1994 and 1998)

b) How many people received food stamps in 1996?

(A: 26 million)

(A: 1 sec)

- **13**. a) Write a quadratic equation in standard form whose solutions are -3 and 7.
- b) Write a quadratic equation in standard form with integer coefficients whose solutions are -1/2 and 3/5.

Polynomial Equations and Their Applications

- **1.** James Bond stands on top of a 240-foot building and throws a film canister upward to a fellow agent in a helicopter 16 feet above the building. The height of the film above the ground t seconds later is given by the formula $h = -16^{2} + 32t + 240$ where h is in feet.
 - a) Calculate h(0) and h(1). What is their meaning in this context?
 - b) How long will it take the film canister to reach the agent in the helicopter?
 - c) If the agent misses the canister, when will it pass James Bond on the way down? (A: 2 sec)
 - d) How long will it take to hit the ground? (A: 5 sec)
- 2. Textbook # 72 page 373. A rectangular parking lot has a length that is 3 yards greater than the width. The area of the parking lot is 180 square yards. Find the length and width.

 (A: 15 yd; 12 yd)
- 3. <u>Textbook #78 page 374</u> As part of a landscaping project, you put in a flower bed measuring 20 feet by 30 feet. To finish off the project, you are putting in a uniform border of pine bark around the outside of the rectangular garden. You have enough pine bark to cover 336 square feet. How wide should the border be? (A: 3 ft)
- **4.** The size of a rectangular computer monitor screen is given by the length of its diagonal. If the length of the screen should be 3 inches greater than its width, what are the dimensions of a 15-inch monitor? (A: 9in by 12 in)
- **5.** Textbook #83 page 374

A tree is supported by a wire anchored in the ground 15 feet from its base. The wire is 4 feet longer than the height that it reaches on the tree. Find the length of the wire.

(A: 30 1/8 ft)

6. The height, h, of a baseball t seconds after being hit is given by $h = -16t^2 + 64t + 4$. When will the baseball reach a height of 64? (A: 3/2, 5/2 sec)

7. Textbook #80 page 374

A machine produces open boxes using square sheets of metal. The machine cuts equal-sized squares measuring 3 inches on a side from the corners and then shapes the metal into an open box by turning up the sides. If each box must have a volume of 75 cubic inches, find the length and width of the open box.

(A: 5 in)

8. A car traveling at 50 feet per second (about 34 mi per hour) can stop in 2.5 seconds after applying the brakes hard. The distance the car travels in feet, t seconds after applying the brakes is $d = 50t - 10t^2$. How long does it take the car to travel 40ft? (A: 1 second)