## Chapter 10 - Trigonometry of Right Triangles <br> Trigonometric Ratios - Applications

1. A giant redwood tree casts a shadow 532 ft long.

Find the height of the tree if the angle of elevation of the sun is $25.7^{\circ}$.
2. From a point on the ground 500 feet from the base of a building, it is observed that the angle of elevation to the top of the building is $24^{\circ}$ and the angle of elevation to the top of a flagpole atop the building is $27^{\circ}$. Find the height of the building and the length of the flagpole.
3. Find $\sin \alpha, \cos \beta, \tan \alpha, \cot \beta$ if
4. Find the side labeled $x$.

5. Find $x$ correct to five decimal places.

6. Sketch a right triangle that has one acute angle $\theta$, and find the other five trigonometric ratios of $\theta$.
a) $\sin \theta=\frac{3}{5}$
b) $\tan \theta=\sqrt{3}$
7. Express $x$ and $y$ in terms of trigonometric ratios of $\theta$.

8. Evaluate the expressions:
a) $\sin 30^{\circ}+\cos 30^{\circ}$
b) $\sin 30^{\circ} \csc 30^{\circ}$
c) $\left(\sin 60^{\circ}\right)^{2}+\left(\cos 60^{\circ}\right)^{2}$
9. Solve the right triangle.

10. Using a protractor, sketch a right triangle that has the acute angle $40^{\circ}$. Measure the sides carefully and use your results to estimate the six trigonometric ratios of $40^{\circ}$.
11. Use a ruler to carefully measure the sides of the triangle, and then use your measurements to estimate the six trigonometric ratios of $\theta$.

12. From the top of a $200-\mathrm{ft}$ lighthouse, the angle of depression to a ship in the ocean is $23^{\circ}$. How far is the ship form the base of the lighthouse?
13. A 20 -ft ladder leans against a building so that the angle between the ground and the ladder is $72^{\circ}$. How high does the ladder reach on the building?
14. A man is lying on the beach, flying a kite. He holds the end of the kite string at ground level, and estimates the angle of elevation of the kite to be $50^{\circ}$. If the string is 450 ft long, how high is the kite above the ground?
15. A water tower is located 325 ft from a building. From a window in the building, it is observed that the angle of elevation to the top of the tower is $39^{\circ}$ and the angle of depression to the bottom of the tower is $25^{\circ}$. How tall is the tower? How high is the window?
16. An airplane flying at the rate of 350 feet per second begins to climb at an angle of $10^{\circ}$. What is the increase in altitude over the next 15 seconds if the speed remains the same?
17. At an altitude of $12,000 \mathrm{ft}$, a pilot sees two towns through angles of depression of $37^{\circ}$ and $48^{\circ}$. To the nearest ten feet, how far apart are the towns?
18. To estimate the height of a mountain above a level plain, the angle of elevation to the top of the mountain is measured to be $32^{\circ}$. One thousand feet closer to the mountain along the plain, it is found that the angle of elevation is $35^{\circ}$. Estimate the height of the mountain.
19. When the moon is exactly half full, the earth, moon, and the sun form a right angle (moon at the right angle).At that time the angle formed by the sun, earth, and moon is measured to be $89.85^{\circ}$. If the distance from the earth to the moon is $240,000 \mathrm{mi}$, estimate the distance from the earth to the sun.
20. Find x correct to one decimal place.


