

Indefinite Integrals

Everywhere in the table below, I is an interval included in the real number set R and C is the set of all constant functions defined on I with real values.

1	$f : R \rightarrow R,$ $f(x) = x^n; n \in N$	$\int x^n dx = \frac{x^{n+1}}{n+1} + C$
2	$f : I \rightarrow R; I \subset (0, \infty),$ $f(x) = x^a; a \in R \setminus \{-1\}$	$\int x^a dx = \frac{x^{a+1}}{a+1} + C;$ $\int dx = x + C$
3	$f : R \rightarrow R,$ $f(x) = a^x; a \in R_+ \setminus \{1, 0\}$	$\int a^x dx = \frac{a^x}{\ln a} + C;$ $\int e^x dx = e^x + C$
4	$f : I \rightarrow R; I \subset R \setminus \{0\},$ $f(x) = \frac{1}{x}$	$\int \frac{1}{x} dx = \ln x + C$
5	$f : R \rightarrow R,$ $f(x) = \sin x$	$\int \sin x dx = -\cos x + C$
6	$f : R \rightarrow R,$ $f(x) = \cos x$	$\int \cos x dx = \sin x + C$
7	$f : I \rightarrow R; I \subset R \setminus \left\{ (2k+1) \frac{\pi}{2} \mid k \in Z \right\}$ $f(x) = \sec^2 x$	$\int \sec^2 x dx = \tan x + C$
8	$f : I \rightarrow R; I \subset R \setminus \{kp \mid k \in Z\},$ $f(x) = \csc^2 x$	$\int \csc^2 x dx = -\cot x + C$
9	$f : I \rightarrow R; I \subset R \setminus \left\{ (2k+1) \frac{\pi}{2} \mid k \in Z \right\}$ $f(x) = \sec x \tan x$	$\int \sec x \tan x dx = \sec x + C$
10	$f : I \rightarrow R; I \subset R \setminus \{kp \mid k \in Z\},$ $f(x) = \csc x \cot x$	$\int \csc x \cot x dx = -\csc x + C$
11	$f : I \rightarrow R; I \subset (-a, a), a > 0$ $f(x) = \frac{1}{\sqrt{a^2 - x^2}}$	$\int \frac{1}{\sqrt{a^2 - x^2}} dx = \sin^{-1} \frac{x}{a} + C;$ $\int \frac{1}{\sqrt{1 - x^2}} dx = \sin^{-1} x + C$
12	$f : R \rightarrow R$ $f(x) = \frac{1}{x^2 + a^2}; a \neq 0$	$\int \frac{1}{x^2 + a^2} dx = \frac{1}{a} \tan^{-1} \frac{x}{a} + C;$ $\int \frac{1}{x^2 + 1} dx = \tan^{-1} x + C$
13	$f : I \rightarrow R; I \subset (-\infty, -1) \cup (1, \infty)$ $f(x) = \frac{1}{ x \sqrt{x^2 - 1}}$	$\int \frac{1}{ x \sqrt{x^2 - 1}} dx = \sec^{-1} x + C$
14	$f : I \rightarrow R; I \subset R \setminus \left\{ (2k+1) \frac{\pi}{2} \mid k \in Z \right\}$ $f(x) = \tan x$	$\int \tan x dx = -\ln \cos x + C$
15	$f : I \rightarrow R; I \subset R \setminus \{kp \mid k \in Z\}$ $f(x) = \cot x$	$\int \cot x dx = \ln \sin x + C$
16	$f : I \rightarrow R; I \subset R \setminus \left\{ (2k+1) \frac{\pi}{2} \mid k \in Z \right\}$ $f(x) = \sec x$	$\int \sec x dx = \ln \sec x + \tan x + C$
17	$f : I \rightarrow R; I \subset R \setminus \{kp \mid k \in Z\}$ $f(x) = \csc x$	$\int \csc x dx = -\ln \csc x + \cot x + C$

