## VERTICAL SHIFTING

## Exercise \#1

Use the graph of

$$
f(x)=x^{2}
$$

to obtain the graphs of

$$
g(x)=x^{2}+1
$$

and

$$
h(x)=x^{2}-2 .
$$



| Equation | How to obtain the graph | Example |
| :---: | :---: | :---: |
| $y=f(x)+k$ <br> $k>0$ | Shift graph of $y=f(x)$ upward $k$ units. | $g(x)=x^{2}+1$ |
| $y=f(x)-k$ <br> $k>0$ | Shift graph of $y=f(x)$ downward $k$ units. | $h(x)=x^{2}-2$ |

## Exercise \#2

Use the graph of

$$
f(x)=|x|
$$

to obtain the graph of
$g(x)=|x|+2$.

## HORIZONTAL SHIFTING

## Exercise \#3

Use the graph of

$$
f(x)=x^{2}
$$

to obtain the graphs of

$$
g(x)=(x-1)^{2}
$$

and

$$
h(x)=(x+1)^{2} .
$$



| Equation | How to obtain the graph | Example |
| :---: | :---: | :---: |
| $y=f(x-h)$ <br> $h>0$ | Shift graph of $y=f(x)$ to the right $h$ units. | $g(x)=(x-1)^{2}$ |
| $y=f(x+h)$ <br> $h>0$ | Shift graph of $y=f(x)$ to the left $h$ units. | $h(x)=(x+1)^{2}$ |

## Exercise \#4

Use the graph of

$$
f(x)=\sqrt{x}
$$

to obtain the graph of $g(x)=\sqrt{x-3}$.


## VERTICAL STRETCH AND COMPRESSION

## Exercise \#5

Use the graph of

$$
f(x)=|x|
$$

to obtain the graphs of

$$
g(x)=2|x|
$$

and

$$
h(x)=\frac{1}{2}|x|
$$



| Equation | How to obtain the graph | Example |
| :---: | :---: | :---: |
| $y=a f(x)$ <br> $a>1$ | Stretch the graph of $y=f(x)$ vertically by a factor of $a$. | $g(x)=2\|x\|$ |
| $y=a f(x)$ <br> $0<a<1$ | Compress the graph of $y=f(x)$ vertically by a factor of $\frac{1}{a} \cdot$ | $h(x)=\frac{1}{2}\|x\|$ |

## HORIZONTAL COMPRESSION AND STRETCH

## Exercise \#6

Use the graph of

$$
f(x)=\sqrt{x}
$$

to obtain the graphs of

$$
g(x)=\sqrt{2 x}
$$

and

$$
h(x)=\sqrt{\frac{1}{2} x}
$$



| Equation | How to obtain the graph | Example |
| :---: | :---: | :---: |
| $y=f(a x)$ <br> $a>1$ | Compress the graph of $y=f(x)$ horizontally by a factor of $a$. | $g(x)=\sqrt{2 x}$ |
| $y=f(a x)$ <br> $0<a<1$ | Stretch the graph of $y=f(x)$ horizontally by a factor of $\frac{1}{a}$. | $h(x)=\sqrt{\frac{1}{2}} x$ |

Exercise \#7

Exercise \#8

Find the function that is finally graphed after the following transformations are applied to $\begin{array}{lll}\text { the graph of } & \text { a) } f(x)=\sqrt{x} ; & \text { b) } g(x)=x^{3} .\end{array}$

1) Shift left 3 units
2) Shift up 1 unit.

The graph of $y=f(x)$ is shown. Sketch the graph of each function:
a) $y=f(2 x)$
b) $y=f\left(\frac{1}{2} x\right)$.



Exercise \#9
The graph of $y=f(x)$ is shown. Sketch the graph of each function:
a) $H(x)=f(x+1)-2$
b) $Q(x)=\frac{1}{2} f(x)$.


Exercise \#10 If $(0,3)$ is a point on the graph of $y=f(x)$, which of the following points must be on the graph of $y=2 f(x)$ ?
a) $(0,3)$
b) $(0,2)$
c) $(0,6)$
d) $(6,0)$.

## REFLECTION ABOUT THE AXES

## Exercise \#11

Use the graph of

$$
f(x)=\sqrt{x}
$$

to obtain the graphs of

$$
g(x)=-\sqrt{x}
$$

and

$$
h(x)=\sqrt{-x}
$$



| Equation | How to obtain the graph | Example |
| :---: | :---: | :---: |
| $y=-f(x)$ | Reflect the graph of $y=f(x)$ about the $x$-axis. | $g(x)=-\sqrt{x}$ |
| $y=f(-x)$ | Reflect the graph of $y=f(x)$ about the $y$-axis. | $h(x)=\sqrt{-x}$ |

Exercise \#12 Graph each function using the techniques of shifting, compressing, stretching, and/or reflecting. Start with the graph of the basic function and show all stages.
a) $f(x)=\frac{1}{-x}+2$
b) $g(x)=-(x+1)^{3}-1$

