

REVIEW TEST #2

Chapters 4, 5, and 6 (6.1, 6.2)



Test #2 will be
Wednesday, Nov. 7

You should know the following:

- how to graph the basic functions sin, cos, tan, cot, sec, csc
- domain, range, period, amplitude (when defined) and vertical asymptotes (when applicable) for the basic functions
- how to graph transformations of trigonometric functions (vertical translations, vertical stretching and compression, horizontal stretching and compression, horizontal shifting)
- how to graph the inverse sine, inverse cosine, and inverse tangent functions
- domain and range for the inverse functions
- evaluate the inverse sine, cosine, and tangent functions
- compose trigonometric functions and their inverses
- prove trigonometric identities
- solve trigonometric equations

IMPORTANT FORMULAS

- $\tan x = \frac{\sin x}{\cos x}$
- $\cot x = \frac{1}{\tan x} = \frac{\cos x}{\sin x}$
- $\sec x = \frac{1}{\cos x}$
- $\csc x = \frac{1}{\sin x}$
- $\sin^2 x + \cos^2 x = 1$
- sine and cosine functions have period $2\mathbf{p}$

$$\sin(x + 2k\mathbf{p}) = \sin x$$

$$\cos(x + 2k\mathbf{p}) = \cos x$$
- tangent function has period \mathbf{p}

$$\tan(x + k\mathbf{p}) = \tan x$$
- $\cos(a + b) = \cos a \cos b - \sin a \sin b$
- $\cos(a - b) = \cos a \cos b + \sin a \sin b$
- $\sin(a + b) = \sin a \cos b + \sin b \cos a$
- $\sin(a - b) = \sin a \cos b - \sin b \cos a$
- $\cos 2a = \cos^2 a - \sin^2 a$
- $\cos 2a = 2\cos^2 a - 1$
- $\cos 2a = 1 - 2\sin^2 a$
- $\sin 2a = 2\sin a \cos a$

OTHER FORMULAS

$$\sin(x + \mathbf{p}) = -\sin x$$

$$\cos(x + \mathbf{p}) = -\cos x$$

$$\cos(-x) = \cos x \quad \text{cosine is an even function}$$

$$\sin(-x) = -\sin x \quad \text{sine is an odd function}$$

$$\tan(a + b) = \frac{\tan a + \tan b}{1 - \tan a \tan b}$$

$$\tan(a - b) = \frac{\tan a - \tan b}{1 + \tan a \tan b}$$

$$\tan 2a = \frac{2\tan a}{1 - \tan^2 a}$$

$$\cos a = \pm \sqrt{\frac{1 + \cos 2a}{2}}$$

$$\sin a = \pm \sqrt{\frac{1 - \cos 2a}{2}}$$

To prepare for the test, study the following:

All problems done in class + Quiz #2

Homework #4	Section 4.1	7, 8, 11 – 24 , 51, 53, 55, 57
	Section 4.2	1, 4, 7, 13, 17, 20, 21, 23, 30, 33 – 36, 41, 42, 44, 46, 47, 48
	Section 4.3	1, 4, 7, 10, 11, 14, 15, 18, 19, 29, 33, 34 37, 47, 49
	Section 4.5	7, 13, 20, 23, 24

Homework #5	Section 4.6	all
	Section 5.1	all
	Section 5.2	1 – 7 odd, 21 – 29 odd, 53, 55
	Section 5.3	all
	Section 5.5	1, 3, 5, 7, 9, 11

Sections 6.1 & 6.2 Study all exercises done in class. For more practice, do some of the odd problems from the book: 6.1 (1 – 37, 47 – 53), 6.2 (1 – 37, 47 – 57)

- 1) Find a formula for $\tan(a+b)$ and $\tan(a-b)$ in terms of $\tan a$ and $\tan b$.
- 2) Find a formula for $\sin 3a$ in terms of $\sin a$.
- 3) Find a formula for $\cos 3a$ in terms of $\cos a$.
- 4) Express each of the following in terms of x : $\cos(\sin^{-1} x)$, $\sin(\cos^{-1} x)$, $\cos(\tan^{-1} x)$, $\sin(\tan^{-1} x)$, $\tan(\cos^{-1} x)$, $\tan(\sin^{-1} x)$.